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## Comparative Assessment of Methods for Forecasting River Runoff with Different Conditions of Organization.

Fedor N Lisetskii\*, Vitaliy I Pichura, Yaroslava V Pavlyuk, and Olga A Marinina.

Belgorod State University, Russia, 308015, Belgorod, Pobedy str., 85.

### ABSTRACT

The article presents the results of comparative analysis of application of traditional statistical methods and non-linear multilayer neural networks for processing multi-year data of the river runoff with the aim of its forecasting. It has been shown that universal possibilities are possessed by neuromodels based on multilayer perceptron (MLPN), that have provided test sampling reliability of modeling of 82–93%. The obtained in the work optimal parameters for learning predictive neuronetworks are recommended for learning transformation and forecast of river runoff in the situation of permanent anthropogenic influence on basin.

**Key words:** neuron networks, Box-Jenkins method, Winters method, river runoff, modeling, forecasting.

*\*Corresponding author*

**INTRODUCTION**

The actual problem of using water resources is the improvement of method of analysis of river runoff assessment under fluctuated natural-economic conditions. The methods of statistical modeling and forecasting allow to get the most probable scenarios of random processes. The major part of series, including series with trend-cycling, seasonal (non-regular) components is possible to be described by autoregressive integrated moving average model (ARIMA). It is flexible enough and covers a wide range of stationary and non-stationary processes [1]. Seasonal components make it possible to take Winters method into account (Three-PES – three-parameter exponential soothing). But noisy and distorted information puts difficulties in the way of getting reliable forecasts. Artificial Neural Networks (ANN) allow to successfully solve problems which one cannot do via traditional methods [2]. Various approaches and results of possibilities of ANN applications have been studied by ASCE Task Committee [3], including flood forecast depending on precipitation total and catch water basin [4, 5], the modeling of within-year, annual river runoff for different climatic conditions, analysis of hydrochemical regime of the rivers [6-9].

**METHODS**

Similarity of multi-year fluctuation in the river runoff has been studied using non-parameter methods: Kendall coordination and Spearman correlation. The rivers have been identified and grouped according to similar conditions of runoff organization using the method of difference integral curves. The methods of Box-Jenkins, Winters and multilayer ANN (RBFTN – radial basis, MLPN – multilayer perceptions) have been used for comparative forecasting of the river runoff movement. Instruction of ANN with input data and correction of weight factors is by means of back propagation of error algorithm (BFGS):

$$w_{ni}(t+1) = \eta \delta_i x_n(t) + \alpha(w_{ni}(t) - w_{ni}(t-1))$$

where  $w_{ni}(t)$  – weight from neuron  $n$  or input signal element  $n$  to neuron  $i$  at the moment of time  $t$ ;  $x_n$  – neuron yield  $n$  or  $n$ 'th element of the signal;  $\eta$  – learning rate coefficient;  $\alpha$  – inertial coefficient;  $\delta_i$  – error of neuron  $i$ .

The error function is difference of current output (approximate values) and ideal output (empirical values) of the network. The mathematical expectation of absolute percentage error is used to cross-check forecasting models (in physical measurements and percentage – MAPE). STATISTICA and Automated Neural Networks for Windows are used for processing.

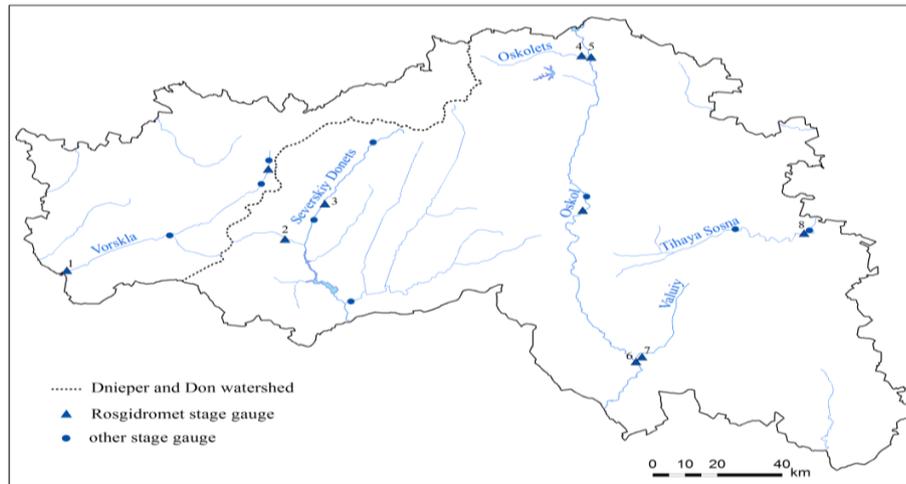
**MAIN BODY**

It has been studied the annual runoff of eight river stations (fig. 1) of the rank V with catch water basin ( $F$ ) that is less than  $800 \text{ km}^2$  and of the rank VI ( $1200 \text{ km}^2 < F < 9000 \text{ km}^2$ ) (see table 1). Duration of series sensing covers 1930–2012 years, standard error value is not  $>10\%$  ( $3\% < \sigma_{w_0} < 7\%$ ), variation coefficient is not  $> 0.5$  ( $0.22 \leq C_v \leq 0.5$ ), variation coefficient error according to moments method is within 8-10.5%. The results of calculated hydrologic characteristic indicate the representativeness of the studied periods of runoff formation.

**Table 1: Statistics of average multi-year water expenditure for the rivers of the region of Belgorod**

Statistical indicators		Rivers <sup>a</sup>							
		1	2	3	4	5	6	7	8
Observations, years	N	81	62	50	63	66	57	60	31
Average consumption, m <sup>3</sup> /s	Q <sub>0</sub>	5.81	1.00	2.57	1.92	6.25	14.36	3.26	5.80
Variation coefficient	C <sub>v</sub>	0.36	0.50	0.32	0.40	0.27	0.22	0.46	0.25
Coefficient of skewness	C <sub>s</sub>	0.67	0.51	0.42	0.57	0.55	0.69	1.40	1.35

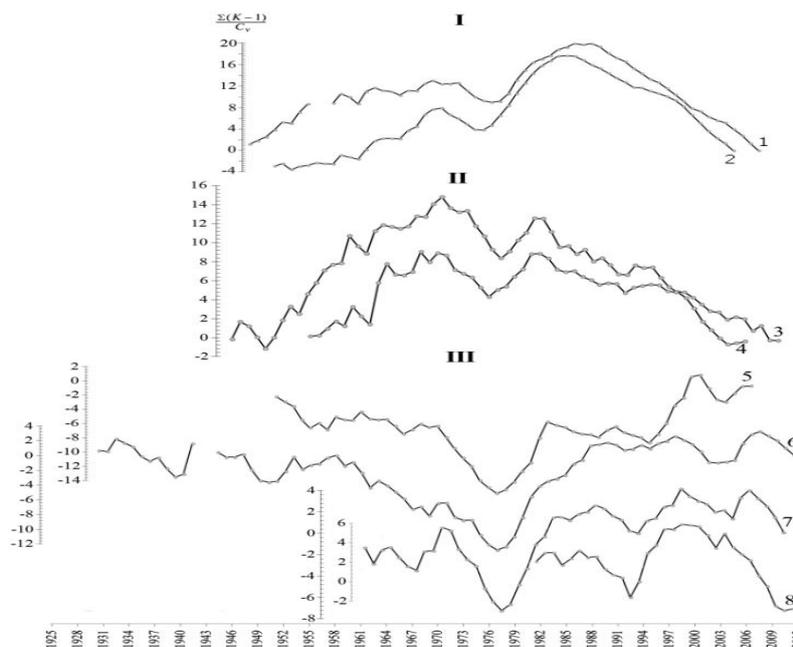
<sup>a</sup> Numbering of hydroposts in fig. 1.



**Figure 1: Rivers runoff observational hydrostations in the region of Belgorod: 1 – Kozinka (Vorskla); 2 – Belgorod (Vezelka); 3 – Kiselevo (Severskiy Donets); 4 – Staryy Oskol (Oskolets); 5 – Staryy Oskol (Oskol); 6 – Razdolye (Oskol); 7 – Valuyki (Valuyki); 8 – Alekseyevka (Tihaya Sosna).**

The analysis of annual expenditure dynamics has shown a certain synchronism in changes of water content of the rivers of the Region of Belgorod, high values of Kendall correlation and ranking order correlation - 0,95 point at this, and it is indicative of runoff isotropism in the explored territory.

Statistical methods of the forecasting have been approbated and compared in terms of characteristic types of annual changes of the river runoffs [10], located on the southwestern slopes of Sredne-Russkaya Vozvyshennost' in the basins of the Dnieper and the Don (see fig. 1). In terms of the analysis of differential integral curves of the annual runoff three groups of rivers (fig. 2), for which characteristic are individual seasonal, cyclic and trend changes and also uneven emissions, depending on natural conditions and hydroeconomic situation of the basin, are differentiated. The first group comprises the rivers of the V rank with indigenous transformation of hydroregimes and water-collecting area of  $F < 500 \text{ km}^2$ ; the second one – the rivers of the VI rank with disturbed type of hydrofunctioning and water-collecting area of  $1000 \text{ km}^2 < F < 1800 \text{ km}^2$ , the rivers of the third group are the rivers with relatively stable type of hydrofunctioning of the Vrank ( $500 \text{ km}^2 < F < 1000 \text{ km}^2$ ) and of the VI rank ( $1800 \text{ km}^2 < F < 9000 \text{ km}^2$ ).



**Figure 2: Mixed differential integral curves of the river runoff:**

$(\Sigma(K-1)/Cv)$  – values of integral curves, where K – ratio of actual condition of the river runoff in a certain period t to mean annual value; Cv – coefficient of annual river runoff variation.

River groups I–III: 1 – Vezelka (rank V, F = 394 km<sup>2</sup>), 2 – Ooskolets (rank V, F = 494 km<sup>2</sup>), 3 – Valuiy (rank VI, F = 1290 km<sup>2</sup>), 4 – Oskol (river sources, rank VI, F = 1540 km<sup>2</sup>), 5 – Oskol (Razdolnye – lower current, rank VI, F = 8640 km<sup>2</sup>), 6 – Vorskla (rank VI, F = 1870 km<sup>2</sup>), 7 – Severskiy Donets (rank V, F = 740 km<sup>2</sup>), 8 – Tihaya Sosna (rank VI, F = 2060 km<sup>2</sup>).

Hydrologic regime using selected methods of forecasting has been modeled by using multiple combining of the parameters and model types. In optimal models (table 2) there is the obtained reflection of the best qualities, that have been gained in terms of learning (80%) and testing (20%) sets.

**Table 2: Comparative assessment of the time analysis methods with the aim of forecasting the average annual rivers runoff**

Method	Model parameters	MAPE, %	
		in terms of learning sample	in terms of testing sample
the I group of the rivers			
ARIMA	$p(1), d(1), q(1), Ps(1), Ds(0), Qs(0)$	16–25	25–32
Three-PES	$\alpha = 0.5; 0.7, \beta = 0.1, \gamma = 0.1$	20–32	24–43
MLPN	Learning algorithm – BFGS Error processing function – SSE Hidden and output neurons activation function – Exponential (range: 0;+∞), Hyperbolic tangent (range: –1;+1), Logistic sigmoid (range: 0;1)	12–18	18–22
the II group of the rivers			
ARIMA	$p(1), d(1), q(0), Ps(0), Ds(0), Qs(1)$	20–25	26–28
Three-PES	$\alpha = 0.1, \beta = 0.1, \gamma = 0.1$	20–32	23–38
MLPN	Learning algorithm – BFGS Error processing function – SSE Hidden and output neurons activation function – Hyperbolic tangent (range: –1;+1), Hyperbolic tangent (range: –1;+1), Exponential (range: 0;+∞)	7–14	16–18
The III group of the rivers			
ARIMA	$p(1), d(1), q(1), Ps(1), Ds(0), Qs(0)$	25–27	30–35
Three-PES	$\alpha = 0.5; \beta = 0.1, \gamma = 0.1$	30–32	34–38
MLPN	Learning algorithm – BFGS Error processing function – SSE Hidden and output neurons activation function – Logistic sigmoid (range: 0;1), Hyperbolic tangent (range: –1;+1), Exponential (range: 0;+∞), Identity (range: –∞;+∞)	7–10	7–18
The I–III groups of the rivers			
RBFTN	Learning algorithm – RBFTN Error processing function – SSE Hidden neurons activation function – Gaussian Output neuron signal function – Identity (range: –∞;+∞)	Group I (19–21) Group II (30–32) Group III (20–34)	Group I (22–30) Group II (35–40) Group III (20–40)

Abbreviations: MAPE – mathematical expectation of absolute error; MLPN – Multilayer Perceptron Network; RBFTN – Radial Basis Function Training Network; SSE – sum-squares error function, BFGS – Broyden-Fletcher-Goldfarb-Shanno.

The analysis of table 2 shows the advantage of ANN with architecture of MLPN. The realization of ANN for a definite aim (quantity of layers, hidden neurons, neuron activation functions, size of input set) depends on hydrologic characteristics of the rivers and the degree of their disturbance. The main feature of ANN-modelling is in its being based only on initial data without efforts to attract a priori reasons.

The most reliable runoff forecasting can be provided for the rivers with defined natural cyclicity in terms of water basin > 1000 km<sup>2</sup>. For the rivers of group I the reliability of forecasting of MLPN based on testing sample is 81.9%. Runoff fluctuation under the influence of anthropogenic loads determines the

optimal period of water content of the rivers. For group I it should not exceed the period of 8–9 years. For the river content forecasting of group II the initial interval should exceed the period of 12–18 years, then the reliability of forecasting of MLPN in terms of testing sample reaches 84.3%. To create effective neuromodels of the forecasting of the river runoff of group III with stable type of hydrofunctioning ( $1800 \text{ km}^2 < F < 9000 \text{ km}^2$ ) input time interval should be equal to or exceed three minor cycles ( $> 27$  years), for rivers of  $500 \text{ km}^2 < F < 1000 \text{ km}^2$  it should be equal to or exceed one minor cycle (8–9 years and more), maximum reliability of forecasting of MLPN in terms of testing sample is 92.7%. For the rivers of group III the forecasting is carried out for long-term period ( $> 15$  years). The reference period of time series should be 2–3 times greater than predictive period.

Non-linear multilayer ANN have been created to forecast changes in dynamics of the river water content. Forecasting error in terms of testing sample is 7-18% that proves a high degree of reliability of the obtained data of the river runoff modelling within the time period.

### CONCLUSION

Comparative analysis of application of traditional statistic methods (ARIMA, Three-PES) and non-linear multilayer ANN (RBFTN, MLPN) has shown that ANN with the architecture of multilayer perception have the advantage in solving the problem of river runoff. Specifics of aged dynamics of the annual change of the river runoff on hydrological posts in the Dnieper and Don basins are conditioned by differences in hierarchy (rank) of the rivers, their water catchment area and degree of hydrological regime disturbance. On the basis of methods of non-parameter statistics it has been determined non-linear connection of synchronism of river water content with different types of hydrological functioning. By the results of differential integral curves of annual runoff the three types of rivers with specific seasonal, cyclic and trend regularities have been determined. For the river runoff forecast as optimal multilayer perception neuromodels (MLPN) have been determined. The reliability of the neuromodels in terms of testing samples is 82–93%. The present optimal variants of input set use for learning expected neuronetworks can be applied for learning transformation and high accuracy forecasting of the river runoff with different types of hydrological functioning in undiminishing anthropogenic influence on catch basins.

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